Prediction of Body Weight from Testicular and Morphological Characteristics in Indigenous Mengali Sheep of Pakistan using Factor Analysis Scores in Multiple Linear Regression Analysis

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ABSTRACT

The objective of the investigation was to predict body weight (BW) from testicular and morphological characteristics of the indigenous Mengali Sheep in Balochistan, Pakistan. The characteristics recorded were: body weight (BW), testicular length (TL), scrotal length (SL), scrotal circumference (SC), body length (BL), withers height (WH) and heart girth (HG) of 107 indigenous Mengali sheep in age range of 12 to 48 months. Only multiple linear regression analysis fitting to the available data showed tendency to multicollinearity problem with VIF >10 and didn’t present optimal solutions. With the purpose of removing the multicollinearity problem and especially making more correct interpretation biologically, the data were exposed to a combination of Factor and Multiple Linear Regression analyses. The appropriateness of factor analysis for the current data was determined by using criteria such as Kaiser-Meyer Olkin (KMO) measure of sampling adequacy and Bartlett’s test of sphericity. These criteria showed that the data were appropriate for the factor analysis, one of the multivariate statistical analysis techniques. Thereafter, the factor analysis was applied to explanatory variables in order to derive new-uncorrelated latent explanatory variables from the variables. In the factor analysis, three new latent variables whose eigenvalues were greater than one were considered as explanatory variable for multiple linear regression analysis. Results obviously illustrated that 79.1% of variation in body weight was effectively explained by these new latent explanatory variables. Consequently, if confirmed at genetic level, the testicular and body traits might provide a significant contribution in the genetic improvement of the body weight of the indigenous Mengali for sheep breeding. © 2012 Friends Science Publishers

Key Words: Factor analysis; Multiple linear regression analysis; Indigenous mengali sheep; Multicollinearity; Varimax rotation

INTRODUCTION

An assessment of indigenous sheep breeds is significant in terms of germplasm conservation of a country. In the indigenous sheep breeding, the identification of multivariate relationships among age, body weight, testicular characteristics and body measurements is necessary for selecting better animals with the aim of gaining more genetic progress on reproductive yield. Among, testicular characteristics, scrotal circumference and length, and testicular length and diameter, which are influenced by age, body weight and seasonal changes were considered to be indirect selection criteria for more genetic progress in fertility (Karakus et al., 2010; Khan et al., 2010). There is a clear evidence that highly significant relationships between pairs of these more heritable testicular traits were reported in some studies (Bilgin et al., 2004) and especially in a previous report, the existence of strong relationships between sperm quality and testicular traits was particularly pointed out in the literature (Blockey, 1980). Karakus et al. (2010) determined that, the best non-linear functions describing relationship between each testicular trait-time in Norduz lambs at young age were Logistic (with 3 parameters) and Richards’s models. Confirming these studies, Salhab et al. (2001) and Karakus et al. (2010) also underlined the significant effects of age and body weight on testicular traits with the multiple linear regression analysis, which is used to identify the relationship of body weight with some body measurements, prone to multicollinearity problem. One of the most effective methods to remove the problem is to use factor analysis scores for multiple regression analysis in different species as reported by many
authors (Keskin et al., 2007a, b; Cankaya et al., 2009; Eyduran et al., 2009; Ogah et al., 2009; Sangun et al., 2009; Yakubu, 2009; Eyduran et al., 2010).

Body measurements as indicators of breed standards (Pesmen & Yardimci, 2008) provide great convenience for the prediction of body weight without weighbridges (Afolayan et al., 2006; Adeyinka & Mohammed, 2006; Yakubu, 2009). In recent years, there have been a growing number of reports on the prediction of body weight from a variety of body traits measured at different growth periods of sheep (Riva et al., 2004; Afolayan et al., 2006; Kunene et al., 2009; Cam et al., 2010a) and goat (Gül et al., 2005; Khan et al., 2006; Moaen-ud-Din et al., 2006; Rahman, 2007; Cam et al., 2010b). Recently, Tariq et al. (2011) made a detailed study on several morphological, fertility and growth traits for Mengali sheep in Pakistan. However, no available work in the literature is on the definition of complex relationships among age, body weight, testicular and body measurements using a combination of factor analysis with multiple linear regression analysis. Hence, the aim of this investigation was to develop a functional model identifying the multivariate-complex association among age, body weight, testicular and body measurements using factor analysis and Multiple Linear Regression Analysis jointly on indigenous Mengali sheep of the Balochistan, Pakistan.

MATERIALS AND METHODS

The study was conducted on 107 indigenous Mengali sheep male lambs born at the Experimental Station, Centre for Advanced Studies in Vaccinology and Biotechnology (ESC), University of Balochistan, Quetta, Pakistan. Morphological data about testicular measurements [testicular length (TL), scrotal length (SL) and scrotal circumference (SC)] and body measurements (body length (BL), withers height (WH) and heart girth (HG) and body weight (BW) at different ages ranging of 12 to 48 months were collected for predicting body weight of the indigenous Mengali sheep in the current study.

In general, multiple linear regression analysis model (Erturk & Tatlihil, 2010) can be written as:

\[ BW = a + b_1SC + b_2SL + b_3TL + b_4BL + b_5WH + b_6HG + e \]

However, use of factor scores together with multiple linear regression analysis is recommended for removing multicollinearity problem. The appropriateness of factor analysis was determined with Kaiser-Meyer-Olkin (KMO) measure of sampling adequacy and Bartlett's test of sphericity (Sharma, 1996). The basic factor analysis equation in matrix form can be written as:

\[ Z = \lambda F + e \]

Where \( Z \) is a px1 vector of variables, \( \lambda \) is a pxm matrix of factor loadings, F is an mx1 vector of factors and \( e \) is a px1 vector of error or residual factors (Sharma, 1996).

As a result of the differences in the units of variables for factor analysis, the variables were standardized and eigenvalues were estimated by a correlation matrix of variables. VARIMAX rotation was utilized for facilitating interpretation of factor loadings (\( \lambda _i \)). Factor coefficients (\( C_{ij} \)) were used to obtain factor scores for the selected factors in the factor analysis. Factors eigenvalues greater than 1 were included in multiple regression analysis (Tabachnick & Fidell, 2001).

Score values corresponding to the chosen factors were used as explanatory variables to predict body weight of the indigenous Mengali sheep. The multiple linear regression equation for fitting standardized body weight and the following factor score equation can be formulated as below:

\[ BW = a + b_1FS_1 + b_2FS_2 + b_3FS_3 + e \]

Where a, regression constant (it is the value of intercept & its value is zero); \( b_1 \), \( b_2 \) and \( b_3 \) are regression coefficients of Factor Scores (FS). FS is factor score and \( e \) is the error term. The significance of regression coefficients (intercept & slopes) were tested using a t-statistic. The quality criteria of the multiple regression analysis were determined with the help of the coefficient of determination (R²) and Mean Square Error (MSE) (Eyduran et al., 2009; Sakar et al., 2011).

In order to estimate body weight of the indigenous Mengali sheep, the current data were analyzed using factor scores in multiple regression analysis. The effectiveness of multiple regression analysis explaining variation in body weight of the indigenous Mengali sheep was determined using determination coefficient (R²) and Root of Mean Square Error (RMSE) and Variance Inflation Factor (VIF), as an indicator of multicollinearity. The VIF is an index, which measures how much the variance of a coefficient is enlarged due to collinearity. For a reliable multiple linear regression analysis, VIF for all the independent variables should be less than 10 (Karakus et al., 2010; Eyduran et al., 2012).

All the statistical evaluations were performed with MINITAB statistical package program. (www.minitab.com).

RESULTS

Definition of breed traits in a sheep breed is of great importance in the determination of genetically superior animals in selection programs to be conducted for breeding purposes. Generally, knowledge on the relationships among these breed traits plays a significant role in respect of improving selection effectiveness. In the current study, Pearson correlation coefficients between age, testicular and morphological traits of indigenous Mengali sheep were calculated (Table I). All the positive correlation coefficients among these traits were statistically significant at significance level of 0.01.
Multiple linear regression analysis was fitted to the current data with the purpose of predicting body weight from testicular and morphological traits in the indigenous Mengali sheep. A severe Multicollinearity problem was observed for the multiple linear regression analysis, because of very strong correlation coefficients and high VIF values (data not shown). Thus, it has produced much higher standard errors for regression coefficients than expected in the multiple linear regression analysis, because of the multicollinearity problem.

For the prediction of body weight in the indigenous Mengali sheep, factor analysis scores in the multiple regression analysis was applied to the current data, as a superior alternative to remove multicollinearity problem being observed in multiple regression analysis, path analysis and canonic correlation analysis. With the exception of body weight as a dependent variable; all other explanatory variables under the investigation. The values on factor score coefficients, rotated factor loadings and communalities obtained in the result of factor analysis with VARIMAX rotation are depicted in Table II. Results of Kaiser-Meyer Olkin Measure (KMO) measure of Sampling Adequacy Bartlett’s test of Sphericity illustrated that factor analysis was appropriate for the current data (Table II). Number of the most suitable factor for the explanatory variables in factor analysis applied was determined as 3 with magnitude of eigenvalues. In other words, the 3 uncorrelated latent variables (FS1, FS2 & FS3) which were statistically significant. The factor producing the highest factor loading for an explanatory variable was the best factor for this variable. For example, SC, SD and BL among the explanatory variables with high correlations of 0.913, 0.912 and 0.646 provided significant contribution to the composition of Factor 1. Similarly, AGE, TL and SL were the variables that statistically made a greater contribution to Factor 2 compared to the rest. In a similar way, WH and HG also contributed in a considerable amount to Factor 3.

Thereafter, as a result of a combination of factor analysis and multiple linear regression analysis, reliable-unbiased regression coefficients were estimated by removing the multicollinearity problem. Table III illustrates the results of multiple regression analysis with new-explanatory (three latent) variables from factor analysis and body weight (dependent variable) standardized with its own average and standard deviation values. As shown in Table III, 79.1% of variation in body weight was explained by three latent variables, FS1, FS2 and FS3, statistically significant, respectively (P<0.01). As expected biologically, body weight increased with increasing FS1, FS2, and FS3, respectively. In Table II, FS1 was positively-highly correlated with SC, SD and BL. In the same way, Pearson correlations of FS3 with WH and HG were positively found. Mathematically, signs (negative) of Pearson correlation coefficients between FS2 with AGE, TL and SL considerably contributing to Factor 2 (Table II) showed similar tendency with the sign (negative) of regression coefficients of FS2 with Table III. When Tables II and III were taken into consideration, statistical analysis results reflected that, body weight would increase with increasing quantitative traits like SC, SD, BL, AGE, TL, SL, WH and HG, respectively.

**DISCUSSION**

Sheep with high values in respect to SC, SD, BL, AGE, TL, SL, WH and HG were more likely to have high values in body weight. This may also be attributed to the nature of growth-development in sheep, depending upon genetic and environmental factors.

Present results illustrated that 79.1% of variation in body weight was explained by three latent variables, FS1, FS2 and FS3, which were statistically significant. The results were supported by a previous study on Muscovy Duck, where Ogah et al. (2009) observed 84.2% and 63.5% total variation in body weight using various morphological measurements for both male and female ducks, respectively. Sangun et al. (2009) explained 98.4% of variation in body weight from several body measurements in Lizardfish with three latent variables. The explained variation of 75.4% for milk yield using four latent variables derived from some udder traits was reported by Keskin et al. (2007a). In the prediction of carcass weight by three latent variables obtained from body measurements, 83.9% R2 was found in multiple regression analysis (Keskin et al., 2007b). In a previous study about factor and multiple regression analysis conducted to examine relationship between carcass weight and six body measurements (live weight, body length, breast circumference, thigh circumference, shank length & wing length) of 8-weeks old Arbor Acre broiler chickens in a sub-humid environment of Nigeria, Yakubu (2009) revealed that, in the varimax rotated factor analysis, two selected

Table 1: Pearson correlation coefficients between pairs of all traits

<table>
<thead>
<tr>
<th>BW</th>
<th>AGE</th>
<th>TL</th>
<th>SC</th>
<th>SD</th>
<th>SL</th>
<th>WH</th>
<th>BL</th>
</tr>
</thead>
<tbody>
<tr>
<td>AGE</td>
<td>0.933</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>TL</td>
<td>0.809</td>
<td>0.894</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>SC</td>
<td>0.544</td>
<td>0.587</td>
<td>0.716</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>SD</td>
<td>0.546</td>
<td>0.589</td>
<td>0.716</td>
<td>0.999</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>SL</td>
<td>0.721</td>
<td>0.797</td>
<td>0.913</td>
<td>0.786</td>
<td>0.787</td>
<td></td>
<td></td>
</tr>
<tr>
<td>WH</td>
<td>0.677</td>
<td>0.712</td>
<td>0.745</td>
<td>0.585</td>
<td>0.587</td>
<td>0.752</td>
<td></td>
</tr>
<tr>
<td>BL</td>
<td>0.699</td>
<td>0.733</td>
<td>0.813</td>
<td>0.826</td>
<td>0.827</td>
<td>0.839</td>
<td>0.738</td>
</tr>
<tr>
<td>HG</td>
<td>0.741</td>
<td>0.759</td>
<td>0.781</td>
<td>0.727</td>
<td>0.728</td>
<td>0.797</td>
<td>0.793</td>
</tr>
</tbody>
</table>
factors from six independent variables explained 87.53% of the total variability in the body measurements of the chickens. In Norduz lambs, Eyduran et al. (2009) successfully predicted weaning weight (WW) using six body measurements (withers height, body length, chest circumference, leg circumference, body depth & width of chest behind shoulders) measured at weaning period by factor scores in multiple regression model. They found approximately 80% of variation in weaning weight with three latent variables. Eyduran et al. (2010) mentioned that 74.2% and 60.2% of total variation were explained for male and female trout in body weight from several biometrical traits viz. total and fork lengths, body height, head length, adipose fin width and adipose fin length of *Salmo trutta fario* trouts. Similarly, Cankaya et al. (2009) conducted a study with the intention of predicting weaning weight from several body measurements (height at withers, height at rump, body length, chest girth & depth, middle & hind rump width & chest width), at the weaning period from a total of 101 Karayaka lambs and reported that 73.1% of variation in weaning weight was explained with the five uncorrelated latent variables. In the current study, model developed could be sufficient with 79.1% accuracy to explain body weight of the indigenous Mengali sheep. However, this finding with the explained variation of 79.1% obtained in the current study was practically in agreement with some of previous works published on various animal species and breeds (Keskin et al., 2007a & b; Cankaya et al., 2009; Eyduran et al., 2009; Ogah et al., 2009; Eyduran et al., 2010), but higher than the variation proportion mentioned by some authors in various publications (Ogah et al., 2009; Yakubu, 2009; Sangun et al., 2009). The current finding on getting rid of the multicollinearity using joint factor analysis scores in the multiple linear regression analysis definitely supported those reported by the above mentioned authors. These differences may be ascribed to the combined effect of genetic (various rearing systems) and environmental factors, and especially different statistical methods and morphological traits used in all previous studies.

### Table II: Factor analysis results applied for explanatory variables

<table>
<thead>
<tr>
<th>Variable</th>
<th>Factor 1</th>
<th>Factor 2</th>
<th>Factor 3</th>
<th>Communiity</th>
</tr>
</thead>
<tbody>
<tr>
<td>SC</td>
<td>0.913</td>
<td>-0.294</td>
<td>0.259</td>
<td>0.988</td>
</tr>
<tr>
<td>SD</td>
<td>0.912</td>
<td>-0.294</td>
<td>0.261</td>
<td>0.988</td>
</tr>
<tr>
<td>BL</td>
<td>0.646</td>
<td>-0.450</td>
<td>0.511</td>
<td>0.881</td>
</tr>
<tr>
<td>AGE</td>
<td>0.245</td>
<td>-0.857</td>
<td>0.375</td>
<td>0.936</td>
</tr>
<tr>
<td>TL</td>
<td>0.423</td>
<td>-0.804</td>
<td>0.362</td>
<td>0.958</td>
</tr>
<tr>
<td>SL</td>
<td>0.548</td>
<td>-0.663</td>
<td>0.400</td>
<td>0.900</td>
</tr>
<tr>
<td>WH</td>
<td>0.254</td>
<td>-0.396</td>
<td>0.845</td>
<td>0.935</td>
</tr>
<tr>
<td>HG</td>
<td>0.473</td>
<td>-0.430</td>
<td>0.687</td>
<td>0.880</td>
</tr>
<tr>
<td>Variance</td>
<td>2.9125</td>
<td>2.5385</td>
<td>2.0139</td>
<td>7.4649</td>
</tr>
<tr>
<td>%Var</td>
<td>0.364</td>
<td>0.317</td>
<td>0.252</td>
<td>0.933</td>
</tr>
</tbody>
</table>

### Table III: Result of Multiple linear regression analysis for latent variables

<table>
<thead>
<tr>
<th>Predictor</th>
<th>Coefficient</th>
<th>SE coeff</th>
<th>t</th>
<th>P</th>
<th>VIF</th>
</tr>
</thead>
<tbody>
<tr>
<td>FS1</td>
<td>0.22331</td>
<td>0.04502</td>
<td>4.96</td>
<td>0.000</td>
<td>1.0</td>
</tr>
<tr>
<td>FS2</td>
<td>-0.76132</td>
<td>0.04502</td>
<td>-16.91</td>
<td>0.000</td>
<td>1.0</td>
</tr>
<tr>
<td>FS3</td>
<td>0.40220</td>
<td>0.04502</td>
<td>8.93</td>
<td>0.000</td>
<td>1.0</td>
</tr>
</tbody>
</table>

S= 0.465313 R²= 79.1% R² adj= 78.5%

In the identification of multivariate relationships among body weight, testicular and morphological traits, compared to only multiple linear regression analysis; the current model, using factor scores together with multiple linear regression analysis was a better alternative approach from the point of removing multicollinearity problem with 79.1 R² (%) explained for body weight. In conclusion, if verified at genetic level, the current results on these
morphological traits might permit obtaining desirable genetic improvement in the body weight for sheep breeding.

REFERENCES


Erturk, Y.E. and F. Tatlıdil, 2010. The effect of the quality assurance systems certificates on the purchasing behaviors of consumers. 5th Central European Congress on Food. 19th-22nd May 2010, Bratislava, Slovakia


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